

Mandelbrot Sets

Created by Jordan Nakamura

How to use Sage

- Go to: www.sabenb.org in order to access the notebook
- Go to: <http://sagemath.org> in order to download SAGE.
- (Note: You don't need to download SAGE to use it! You can just access the notebook online to use it!)

SAGE API

- <http://www.sagemath.org/doc/reference/>

Definition

- All the complex numbers such that:

$$- \quad Z_{n+1} = Z_n^2 + c$$

– Is bounded.

- i.e. If $|Z_{20}| < 2.0$ then we will assume it is bounded!

– By definition $Z_0 = 0$

- More information on

http://en.wikipedia.org/wiki/Mandelbrot_set

Example

- Complex number $c = 2 + 2i$

$$Z_0 = 0 \quad Z_1 = Z_0^2 + (2 + 2i) \quad Z_2 = Z_1^2 + (2 + 2i) = (2 + 2i)^2 + (2 + 2i) = (2 + 10i)$$

$$Z_3 = (2 + 10i)^2 + (2 + 2i) = (-94 + 42i)$$

$$Z_{20} = (5.8 \times 10^{263801} + 8.9 \times 10^{263801} i)$$

For sake of simplicity, assume $Z_{20} = (40 + 40i)$

$$\text{abs}(Z_{20}) = \sqrt{40^2 + 40^2} = \sqrt{1600 + 1600} = \sqrt{3200} = 56.56$$

For sake of simplicity, assume $Z_{20} = (40 + 40i)$

$$56.56 > 2.0 \quad \text{So it is not bounded.}$$

Example 2

$$C = 0 + 0i$$

$$Z_0 = 0$$

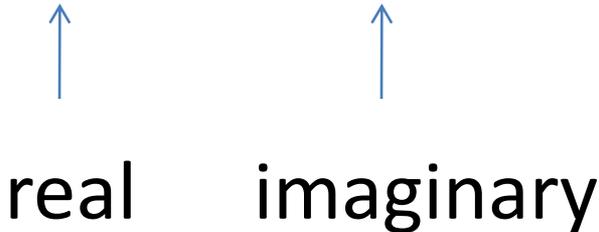
$$Z_{20} = 0^2 + 0i$$

$$\text{abs}(Z_{20}) = \sqrt{0^2 + 0^2} = 0$$

$$0 < 2$$

So it is bounded. Therefore, the point $(0 + 0i)$ is in the Mandelbrot Set.

Complex Plane

- It looks just like the Cartesian coordinate plane, except the “x-axis” is the real numbers and the “y-axis” is the imaginary parts.
- Real numbers are complex numbers without the “imaginary” part.
- Complex number = $2 + 3i$


real imaginary

